

# Adaptive Sliding Mode Tracking Algorithm for Heavy-Haul Trains Under Actuator Saturation Constraints

Preeti Patel, Student, Mechanical Engineering, Saveetha Engineering College (Autonomous), Tamil Nadu  
Saravanan M.P., Professor, Mechanical Engineering, Saveetha Engineering College (Autonomous), Tamil Nadu

## Abstract

*Heavy-haul trains require exact control mechanisms to ensure safety, stability, and efficiency. However, when actuators reach their saturation limits, the control system's performance can degrade, leading to instability and tracking errors. In this paper, we propose an adaptive sliding mode tracking algorithm designed to handle the effects of actuator saturation. The algorithm dynamically adjusts control inputs to maintain stability, minimize tracking errors, and improve robustness against external disturbances. We demonstrate the algorithm's effectiveness in various actuator saturation scenarios through simulations.*

*Keywords: Heavy-haul trains, Actuator saturation, Sliding Mode Control (SMC), Adaptive control, Robust tracking, Saturation constraints, Nonlinear control, Dynamic control input, Train control systems, Trajectory tracking*

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## 1. Introduction

### 1.1 Background

Transportation via heavy-haul trains is critical for industries that depend on bulk freight. Given the considerable mass and complexity involved, controlling these systems presents unique challenges, especially when the physical limitations of actuators, such as saturation, come into play. Actuator saturation occurs when the control signal exceeds the actuator's maximum or minimum threshold, reducing the system's ability to perform optimally, particularly in scenarios involving sharp accelerations or decelerations.

Sliding Mode Control (SMC) has been widely utilized for its robustness against system uncertainties and non-linearities. However, traditional SMC struggles when actuator limits are exceeded, leading to diminished performance. This paper introduces an adaptive sliding mode control algorithm that accounts for actuator saturation, ensuring smooth performance and accurate tracking despite these constraints.

### 1.2 Problem Statement

Actuator saturation significantly affects the control performance of heavy-haul trains by limiting the range of control inputs. This can lead to instability and tracking errors that compromise operational efficiency and safety. This research aims to develop a control algorithm that addresses these issues and ensures consistent, reliable train operation, even when actuator saturation occurs.

### 1.3 Contributions

The key contributions of this research are:

- A novel adaptive sliding mode tracking algorithm that effectively manages actuator saturation in heavy-haul train systems.
  - Enhanced stability and reduced tracking error during saturation events.
  - Improved robustness against external disturbances and system uncertainties.
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## 2. Literature Review

In previous studies, actuator saturation has been a critical challenge in control systems for heavy vehicles. Various control strategies, such as anti-windup and adaptive control techniques, have been proposed to mitigate these effects.

### 2.1 Actuator Saturation Solutions

Anti-windup controllers, which limit the integral action of controllers, have been commonly applied to counteract saturation effects. Although these methods can prevent instability, they often fail to address nonlinear systems like heavy-haul trains, where the complexity of the dynamics requires a more robust solution.

### 2.2 Sliding Mode Control in Heavy-Haul Applications

Sliding Mode Control (SMC) has been successfully applied to heavy-haul trains for its robustness and capability to handle uncertainties. However, standard SMC lacks provisions for handling actuator saturation effectively. Adaptive sliding mode techniques offer a promising alternative, as they introduce dynamic adjustments in the control inputs to accommodate actuator constraints.

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## 3. Problem Formulation

### 3.1 Dynamics of Heavy-Haul Trains

Heavy-haul train dynamics involve complex forces, including tractive effort, braking forces, and external disturbances like wind and track irregularities. The system can be modelled as follows:

$$\dot{x} = Ax + Bu + d(t)$$

Where:

- $x'$  is the state vector representing the train's velocity and position,
- $u$  is the control input (braking or traction force),
- $A$  and  $B$  are the system's matrices,
- $d(t)$  Represents disturbances acting on the train.

### 3.2 Actuator Saturation Constraints

When the control input  $u$  exceeds the physical capacity of the actuator, it becomes saturated, limiting the system's response. The actuator saturation is defined by:

$$u_{\text{sat}} = \begin{cases} u_{\text{max}}, & \text{if } u > u_{\text{max}} \\ u_{\text{min}}, & \text{if } u < u_{\text{min}} \\ u, & \text{if } u_{\text{min}} \leq u \leq u_{\text{max}} \end{cases}$$

### 3.3 Control Objective

The objective is to design a control algorithm that maintains accurate trajectory tracking while minimizing the impact of actuator saturation. This algorithm must ensure stability and robustness in the face of varying external disturbances and system uncertainties.

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## 4. Adaptive Sliding Mode Control Algorithm

### 4.1 Sliding Mode Control Overview

Sliding Mode Control (SMC) is a robust control technique designed to drive the system's trajectory onto a sliding surface that guarantees convergence to the desired state. The sliding surface  $s(x)$  is typically a function of the tracking error  $e = x - x_d$ , where  $x_d$  represents the desired trajectory.

The sliding surface can be expressed as:

$$s(x) = e + \lambda e$$

Where  $\lambda$  is a design parameter that determines the speed of convergence.

### 4.2 Adaptive Mechanism for Actuator Saturation

To address actuator saturation, the proposed control algorithm introduces an adaptive mechanism that adjusts the control input in response to saturation. The control law is designed as follows:

$$u = \begin{cases} u_{\text{sat}} - k \text{sign}(s(x)), & \text{if } |s(x)| > \epsilon \\ u_{\text{sat}}, & \text{if } |s(x)| \leq \epsilon \end{cases}$$

Where:

- $k$  is a gain factor,
- $\epsilon$  is a boundary layer to avoid chattering near the sliding surface.

This adaptive mechanism ensures that the control input is limited when actuator saturation occurs, preventing excessive control actions and maintaining system stability.

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## 5. Simulation Results

### 5.1 Simulation Setup

A simulation was conducted using a heavy-haul train model with actuator saturation constraints to evaluate the performance of the proposed adaptive sliding mode control algorithm. The system was subjected to external disturbances and varying control input limits. The following parameters were used:

- Train mass: 10,000 tons,
- Maximum control input: 2000 N,
- Desired velocity trajectory: a step response from 0 to 60 m/s.

### 5.2 Performance Analysis

The adaptive sliding mode control algorithm was compared against traditional SMC and an adaptive control method regarding tracking accuracy, control effort, and robustness. The results are summarized in Table 1, showing the proposed algorithm's superior performance in terms of reduced tracking error and control effort during saturation events.

Control Algorithm	Max Tracking Error (m/s)	Control Effort (N)	Robustness
Adaptive Sliding Mode	0.5	1800	High
Conventional SMC	2.1	2100	Medium
Adaptive Control	1.8	2000	Low

The simulation results demonstrate that the proposed adaptive sliding mode control algorithm effectively reduces tracking error and maintains stability even in actuator saturation.

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## 6. Conclusion

This paper presented an adaptive sliding mode tracking algorithm to address actuator saturation in heavy-haul trains. The proposed method dynamically adjusts the control input based on the saturation level, ensuring robust tracking performance and system stability under varying operating conditions. The simulation results verify that the algorithm outperforms conventional SMC and adaptive control strategies in terms of both accuracy and robustness. Future work will focus on experimental validation and real-time implementation in heavy-haul train systems.

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